


1	(i)	$\left[\frac{dy}{dx}\right] 4 \times 2 + 3 \text{ or } 11 \text{ isw}$ $9 = \text{their } (4 \times 2 + 3) \times 2 + c$ $y = 11x - 13 \text{ or } y = 11x + c \text{ and } c = -13$ <p>stated isw</p>	<p>M1*</p> <p>M1dep*</p> <p>A1</p> <p>[3]</p>	<p>or $y - 9 = \text{their } (4 \times 2 + 3) \times (x - 2)$</p> <p>or $y - 9 = 11(x - 2)$ isw</p>	
1	(ii)	$\frac{4x^2}{2} + 3x$ $[y =] 2x^2 + 3x + c$ $9 = 2 \times 2^2 + 3 \times 2 + c$ $y = 2x^2 + 3x - 5 \text{ cao}$ <p>(1, 0) and (-2.5, 0) oe cao</p> $x = -\frac{3}{4}$ $y = -\frac{49}{8}$	<p>M1*</p> <p>A1</p> <p>M1dep*</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>[7]</p>	<p>must see “2” and “+ c”; may be earned later eg after attempt to find c</p> <p>must include constant, which may be implied by answer</p> <p>allow first 4 marks for $y = 2x^2 + 3x + c$ and $c = -5$ stated</p> <p>or for $x = 1, y = 0$ and $x = -2.5, y = 0$</p> <p>-6.125 or $-6\frac{1}{8}$</p>	<p>B0 for just stating $x = 1$ and $x = -2.5$</p>

1	(iii)	<p>substitution to obtain [$y =$] $f(2x)$ in polynomial form</p> <p>$y = (2x - 1)(4x + 5)$ or $y = 8x^2 + 6x - 5$ or $y = 2\left(2x + \frac{3}{4}\right)^2 - \frac{49}{8}$</p> <p>$\left(\frac{3}{8}, -\frac{49}{8}\right)$ oe</p>	<p>M1</p> <p>A1FT</p> <p>B1</p> <p>[3]</p>	<p>$f(x)$ must be the quadratic in x with linear and constant term obtained in part (ii), may be in factorised form</p> <p>must be simplified to one of these forms, FT their quadratic in x with linear and constant term obtained in part (ii)</p> <p>or FT their (both non-zero) co-ordinates for minimum point or their quadratic in x with linear and constant term obtained in part (ii)</p>	<p>or their $x = 1 \rightarrow$ their 0.5 and their $x = -2.5 \rightarrow$ their $x = -1.25$</p> <p>hence $y = (2x - 1)(4x + 5)$ FT their x-intercepts from their quadratic in x with linear and constant term obtained in part (ii)</p>
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2	<p>$\left[\frac{dy}{dx} = \right] 32x^3$ c.a.o.</p> <p>substitution of $x = \frac{1}{2}$ in their $\frac{dy}{dx}$</p> <p>grad normal = $\frac{-1}{\text{their } 4}$</p> <p>when $x = \frac{1}{2}$, $y = 4\frac{1}{2}$ o.e.</p> <p>$y - 4\frac{1}{2} = -\frac{1}{4}\left(x - \frac{1}{2}\right)$ i.s.w</p>	<p>M1</p> <p>M1 [= 4]</p> <p>M1</p> <p>B1</p> <p>A1 $y = -\frac{1}{4}x + 4\frac{5}{8}$ o.e.</p>	<p>must see kx^3</p> <p>their 4 must be obtained by calculus</p>
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3	(i)	$\frac{dy}{dx} = 4x^3$ when $x = 2$, $\frac{dy}{dx} = 32$ s.o.i. when $x = 2$, $y = 16$ s.o.i. $y = 32x - 48$ c.a.o.	M1 A1 B1 A1	i.s.w.
3	(ii)	34.481	2	M1 for $\frac{2.1^4 - 2^4}{0.1}$
3	(iii) (A)	$16 + 32h + 24h^2 + 8h^3 + h^4$ c.a.o.	3	B2 for 4 terms correct B1 for 3 terms correct
3	(iii) (B)	$32 + 24h + 8h^2 + h^3$ or ft	2	B1 if one error
3	(iii) (C)	as $h \rightarrow 0$, result \rightarrow their 32 from (iii) (B) gradient of tangent is limit of gradient of chord	1 1	

4	i	6.1	2	M1 for $\frac{(3.1^2 - 7) - (3^2 - 7)}{3.1 - 3}$ o.e.	2
	ii	$\frac{((3+h)^2 - 7) - (3^2 - 7)}{h}$ numerator = $6h + h^2$ $6 + h$	M1 M1 A1	s.o.i.	3
	iii	as h tends to 0, grad. tends to 6 o.e. f.t.from "6"+h	M1 A1		2
	iv	$y - 2 = "6" (x - 3)$ o.e. $y = 6x - 16$	M1 A1	6 may be obtained from 	2
	v	At P, $x = 16/6$ o.e. or ft At Q, $x = \sqrt{7}$ 0.021 cao	M1 M1 A1		3

5	<p>(i) ad of chord = $(2^{3.1} - 2^3)/0.1$ o.e. = 5.74 c.a.o.</p> <p>(ii) rrect use of A and C where for C, $2.9 < x < 3.1$ answer in range (5.36, 5.74)</p>	M1 A1 M1 A1	or chord with ends $x = 3 \pm h$, where $0 < h \leq 0.1$ s.c.1 for consistent use of reciprocal of gradient formula in parts (i) and (ii)	4
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